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VOLUME TABLES FOR TREES OF INTERIOR ALASKA

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The attached volume tables are derived from 695 tree measurements obtained in 1957 and 1960. Nine general areas were sampled north and south of the Alaska Range and on the Kenai Peninsula. Data were gathered for white spruce (Picea glauca), quaking aspen (Populus tremuloides), paper birch (Betula papyrifera), and balsam poplar (Populus balsamifera), including black cottonwood (P. trichocarpa) to a limited extent. Most tree measurements came from randomly located 1/50-acre plots within stands comprising at least one acre of the same type and stand-size class.

Smalian's formula was used to determine cubic-foot volume of sample trees at least 5.0 inches d.b.h. (diameter breast high). Volume was found between a one-foot stump and a minimum merchantable top of 4.0 inches inside bark (d.i.b.). Points of measurement were generally at 8.15-foot intervals.

The International 1/4-inch rule and Scribner rule were used to find board-foot volume of sample trees in 16-foot logs. The minimum d.b.h. of sawtimber-size spruce was 9.0 inches; for hardwoods, 11.0 inches. Limits were from a one-foot stump to a top equaling 40 percent of d.b.h., but not less than 6.0 inches d.i.b. in spruce and 8.0 inches d.i.b. in hardwoods.

Initial plottings of volume classes over $D^2H^{1/2}$ were linear over most of the range except those for paper birch cubic-foot and balsam poplar

^{1/2} The combined variable reported by Spurr where

D = d.b.h. in inches

H = total tree height in feet.

Spurr, Stephen H. Forest Inventory. 476 pp. New York: The Ronald Press Co. 1952.

board-foot. These lines dropped slightly at the upper ends--zones of few data. Variability increased with increasing values of D^2H for all plottings. Since the standard deviation of residuals was proportional to volume and volume proportional to D^2H , the variance of residuals was proportional to $(D^2H)^2$. Therefore, $\frac{1}{(D^2H)^2}$ was used in weighting the equations. Independent variables tested were D^2H , D , D^2 , $1/D^2$, and H .

Cubic-foot and board-foot tree volume equations for the four species were obtained by regression analyses^{2/ 3/}. The F-test indicated that quaking aspen and paper birch data could be pooled. The best predictive equation is footnoted beneath each table in this report. Standard errors of estimate were approximated by (standard error of estimate, weighted form) $\sqrt{(D^2H)}$.

The table presented here with respect to paper birch cubic-foot volume differs from one published by Gregory^{4/} in that: (1) paper birch and quaking aspen data were pooled herein; (2) volume was found by Smalian's formula, not graphically; and, (3) whole-inch d.b.h. classes (e.g., $5.0 \leq 5 < 6.0$), not mid-point classes (e.g., $4.6 \leq 5 < 5.6$) were used.

^{2/} Furnival, George M. Regression routines. Yale School of Forestry and Northeastern Forest Expt. Sta., 28 pp., mimeo. 1961

^{3/} Boles, James N. 40-series--stepwise regression system. Calif. Agr. Expt. Sta., Dept. of Agr. Econ., U. of Calif., Berkeley, 43 pp. dittoed. 1962.

^{4/} Gregory, Robert A. Cubic-foot volume tables for paper birch in Alaska. U. S. Forest Serv., Alaska Forest Res. Ctr., Tech. Note No. 49, 1 p. plus 4 tables. 1960.

Table 1.--Volume table for white spruce in Alaska ^{1/}

(In cubic feet, by Smalian's rule)

| D.b.h. D ₂ | | Total height, H (feet) <u>3</u> | | | | | | | | | | | | | | | | | Basis: | | | | |
|--------------------------|-----|---------------------------------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|--------|-----|-------|------------------------|--|
| | | 30 | 35 | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | 85 | 90 | 95 | 100 | 105 | 110 | 115 | 120 | trees | meas- ured <u>4</u> | |
| Inches | | Number | | | | | | | | | | | | | | | | | | | | | |
| 5 | 1.2 | 1.6 | 1.9 | 2.2 | 2.5 | 2.9 | 3.2 | 3.5 | 3.8 | | | | | | | | | | | | | 18 | |
| 6 | 2.0 | 2.5 | 2.9 | 3.4 | 3.8 | 4.3 | 4.7 | 5.2 | 5.6 | | | | | | | | | | | | | 21 | |
| 7 | 2.9 | 3.5 | 4.1 | 4.7 | 5.3 | 5.9 | 6.5 | 7.1 | 7.7 | 8.4 | 9.0 | | | | | | | | | | | 20 | |
| 8 | 3.9 | 4.7 | 5.5 | 6.2 | 7.0 | 7.8 | 8.6 | 9.4 | 10.1 | 10.9 | 11.7 | 12.5 | | | | | | | | | | 29 | |
| 9 | 5.0 | 6.0 | 7.0 | 8.0 | 8.9 | 9.9 | 10.9 | 11.8 | 12.8 | 13.8 | 14.7 | 15.7 | 16.7 | | | | | | | | | 27 | |
| 10 | 6.3 | 7.5 | 8.7 | 9.9 | 11.1 | 12.2 | 13.4 | 14.6 | 15.8 | 17.0 | 18.1 | 19.3 | 20.5 | 21.6 | | | | | | | | 26 | |
| 11 | | 9.2 | 10.6 | 12.0 | 13.4 | 14.8 | 16.2 | 17.6 | 19.1 | 20.5 | 21.9 | 23.3 | 24.7 | 26.1 | | | | | | | | 23 | |
| 12 | | | 12.7 | 14.3 | 16.0 | 17.6 | 19.3 | 21.0 | 22.6 | 24.3 | 26.0 | 27.6 | 29.3 | 31.0 | 32.6 | | | | | | | 14 | |
| 13 | | | 14.8 | 16.8 | 18.7 | 20.7 | 22.6 | 24.5 | 26.5 | 28.5 | 30.4 | 32.3 | 34.3 | 36.3 | 38.2 | | | | | | | 21 | |
| 14 | | | 17.2 | 19.5 | 21.7 | 24.0 | 26.2 | 28.4 | 30.7 | 32.9 | 35.1 | 37.4 | 39.7 | 41.9 | 44.1 | 46.3 | | | | | | 14 | |
| 15 | | | | 22.3 | 24.9 | 27.5 | 30.0 | 32.6 | 35.2 | 37.7 | 40.2 | 42.8 | 45.4 | 48.0 | 50.5 | 53.0 | | | | | | 11 | |
| 16 | | | | 25.4 | 28.3 | 31.2 | 34.1 | 37.0 | 39.9 | 42.8 | 45.7 | 48.6 | 51.5 | 54.4 | 57.3 | 60.2 | 63.1 | 66.0 | | | | 8 | |
| 17 | | | | | 31.9 | 35.2 | 38.5 | 41.7 | 45.0 | 48.3 | 51.5 | 54.8 | 58.1 | 61.3 | 64.6 | 67.8 | 71.1 | 74.3 | | | | 7 | |
| 18 | | | | | | 39.4 | 43.0 | 46.7 | 50.4 | 54.0 | 57.6 | 61.3 | 65.0 | 68.6 | 72.3 | 75.9 | 79.6 | 83.2 | 86.8 | | | 2 | |
| 19 | | | | | | | 51.9 | 56.0 | 60.1 | 64.1 | 68.2 | 72.3 | 76.3 | 80.4 | 84.4 | 88.5 | 92.5 | 96.5 | | | | 5 | |
| 20 | | | | | | | | 66.5 | 70.9 | 75.4 | 79.9 | 84.4 | 88.9 | 93.3 | 97.8 | 102 | 107 | | | | | 1 | |
| 21 | | | | | | | | 73.2 | 78.1 | 83.0 | 87.9 | 92.9 | 97.8 | 103 | 108 | 113 | 118 | | | | | 2 | |
| 22 | | | | | | | | 80.2 | 85.6 | 91.0 | 96.4 | 102 | 107 | 112 | 118 | 123 | 129 | | | | | 1 | |
| 23 | | | | | | | | 87.5 | 93.4 | 99.3 | 105 | 111 | 117 | 123 | 129 | 135 | 140 | | | | | -- | |
| 24 | | | | | | | | | 102 | 108 | 114 | 121 | 127 | 134 | 140 | 146 | 153 | | | | | 1 | |
| 25 | | | | | | | | | 110 | 117 | 124 | 131 | 138 | 145 | 152 | 159 | 166 | | | | | -- | |
| 26 | | | | | | | | | 119 | 126 | 134 | 142 | 149 | 156 | 164 | 171 | 179 | | | | | -- | |
| 27 | | | | | | | | | 128 | 136 | 144 | 152 | 160 | 168 | 176 | 184 | 193 | | | | | -- | |
| 28 | | | | | | | | | 137 | 146 | 155 | 164 | 172 | 181 | 190 | 198 | 207 | | | | | -- | |
| 29 | | | | | | | | | 148 | 157 | 166 | 175 | 185 | 194 | 203 | 212 | 222 | | | | | -- | |

^{1/} From weighted regression: $V = -0.69934 + 0.002, 129, 464, 6 D^2 H$.Standard error of estimate around mean volume ± 2.08 cu.ft. $\pm 9.7\%$; $R^2 = 0.983$.

Volume, inside bark, between a one-foot stump and a minimum merchantable top of 4.0 inches inside bark.

^{2/} Whole-inch class (e.g., $11.0 \leq 11 < 12.0$)^{3/} Mid-point class (e.g., $57.6 \leq 60 < 62.6$)^{4/} Lines contain basic data for 251 trees at least 5.0 inches d.b.h.

Table 2.--Volume table for white spruce in Alaska ^{1/}
(In board feet, International 1/4-Inch)

| D.b.h. D ^{2/} | | Total height, H (feet) ^{3/} | | | | | | | | | | | | | | | | Basis: : trees : meas- : ured ^{4/} | | | |
|---------------------------|----|--------------------------------------|-----|-----|-----|-----|-----|-----|-----|-----|-------|-------|-------|-------|-------|-------|-------|--|-----|--------|--|
| Inches | | 35 | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | 85 | 90 | 95 | 100 | 105 | 110 | 115 | 120 | Number | |
| 9 | 13 | 20 | 26 | 32 | 38 | 44 | 51 | 57 | 63 | 69 | 75 | 82 | | | | | | | | 27 | |
| 10 | 16 | 24 | 31 | 39 | 46 | 54 | 62 | 69 | 77 | 84 | 92 | 99 | 107 | | | | | | | 26 | |
| 11 | 21 | 31 | 40 | 49 | 58 | 67 | 76 | 85 | 94 | 103 | 112 | 121 | 130 | | | | | | | 23 | |
| 12 | | 40 | 51 | 61 | 72 | 83 | 93 | 104 | 115 | 126 | 136 | 147 | 158 | 168 | | | | | | 14 | |
| 13 | | 50 | 63 | 76 | 88 | 101 | 113 | 126 | 138 | 151 | 163 | 176 | 188 | 201 | | | | | | 21 | |
| 14 | | 63 | 78 | 93 | 107 | 121 | 136 | 150 | 165 | 179 | 193 | 208 | 222 | 236 | 251 | | | | | 14 | |
| 15 | | | 94 | 111 | 128 | 144 | 160 | 177 | 193 | 210 | 226 | 242 | 259 | 275 | 292 | 308 | | | | 11 | |
| 16 | | | 113 | 131 | 150 | 169 | 187 | 206 | 224 | 243 | 262 | 280 | 299 | 318 | 336 | 355 | 373 | | | 8 | |
| 17 | | | | 153 | 174 | 195 | 216 | 237 | 258 | 279 | 300 | 321 | 342 | 363 | 384 | 404 | 425 | | | 7 | |
| 18 | | | | | 200 | 223 | 247 | 270 | 294 | 317 | 340 | 364 | 387 | 410 | 434 | 457 | 481 | 504 | | 2 | |
| 19 | | | | | | | 280 | 306 | 332 | 358 | 384 | 410 | 436 | 462 | 488 | 514 | 540 | 566 | | 5 | |
| 20 | | | | | | | | 372 | 400 | 429 | 458 | 487 | 515 | 544 | 573 | 602 | 631 | | | 1 | |
| 21 | | | | | | | | 414 | 446 | 477 | 509 | 541 | 572 | 603 | 635 | 667 | 698 | | | 2 | |
| 22 | | | | | | | | 458 | 493 | 528 | 563 | 597 | 631 | 666 | 701 | 735 | 770 | | | 1 | |
| 23 | | | | | | | | 505 | 543 | 581 | 618 | 656 | 694 | 732 | 769 | 807 | 845 | | | -- | |
| 24 | | | | | | | | | 594 | 636 | 677 | 718 | 759 | 800 | 841 | 882 | 923 | | | 1 | |
| 25 | | | | | | | | | 649 | 694 | 738 | 782 | 826 | 871 | 916 | 960 | 1,005 | | | -- | |
| 26 | | | | | | | | | 705 | 753 | 801 | 849 | 897 | 946 | 994 | 1,042 | 1,090 | | | -- | |
| 27 | | | | | | | | | 764 | 816 | 868 | 920 | 971 | 1,023 | 1,074 | 1,126 | 1,178 | | | -- | |
| 28 | | | | | | | | | 825 | 881 | 936 | 991 | 1,047 | 1,102 | 1,158 | 1,213 | 1,269 | | | -- | |
| 29 | | | | | | | | | 888 | 948 | 1,007 | 1,066 | 1,126 | 1,185 | 1,245 | 1,304 | 1,364 | | | -- | |

^{1/} From weighted regression: $V = -67.1116 + 0.013,663,011 D^2 H + 3344.33/D^2$

Standard error of estimate around mean volume ± 19.2 bd. ft. $\pm 12.1\%$; $R^2 = 0.951$.

Volume, in 16-foot logs, between a one-foot stump and a merchantable top equal to 40% of d.b.h. but not less than 6.0 inches inside bark.

^{2/} Whole-inch class (e.g., 11.0 \leq 11 < 12.0).

^{3/} Mid-point class (e.g., 57.6 \leq 60 < 62.6).

^{4/} Lines contain basic data for 162 trees at least 9.0 inches d.b.h.

Table 3.--Volume table for white spruce in Alaska^{1/}

(In board feet, Scribner)

| D.b.h. D ² / | | Total height, H (feet) ^{3/} | | | | | | | | | | | | | | | | Basis: trees meas- ured ^{4/} | | Number |
|----------------------------|---|--------------------------------------|------|------|------|------|-----|------|------|------|------|------|------|-------|-------|-------|-------|--|-----|--------|
| : | : | 35 | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | 85 | 90 | 95 | 100 | 105 | 110 | 115 | 120 | |
| 9 | | (10) | (16) | (21) | (26) | (30) | 40 | (44) | (47) | (50) | (53) | (56) | (59) | | | | | | | 27 |
| 10 | | (13) | (20) | (28) | (35) | (42) | 49 | 52 | 55 | 58 | 61 | 64 | 67 | 70 | | | | | | 26 |
| 11 | | (16) | (26) | (34) | (42) | (51) | 59 | 64 | 69 | 74 | 80 | 85 | 90 | 95 | | | | | | 23 |
| 12 | | | (31) | (42) | 54 | 62 | 69 | 77 | 84 | 92 | 100 | 107 | 115 | 123 | 130 | | | | | 14 |
| 13 | | | (36) | 50 | 60 | 70 | 80 | 91 | 101 | 111 | 122 | 132 | 142 | 152 | 163 | | | | | 21 |
| 14 | | 40 | 54 | 67 | 80 | 93 | 106 | 122 | 138 | 154 | 170 | 187 | 203 | 219 | 235 | 251 | 267 | | | 14 |
| 15 | | | 58 | 74 | 90 | 106 | 122 | 139 | 159 | 178 | 197 | 217 | 236 | 256 | 275 | 294 | 314 | 333 | | 11 |
| 16 | | | 62 | 81 | 101 | 120 | 139 | 158 | 180 | 203 | 226 | 249 | 272 | 294 | 317 | 340 | 363 | 386 | | 8 |
| 17 | | | | 89 | 112 | 135 | 158 | 177 | 203 | 230 | 256 | 283 | 309 | 336 | 362 | 388 | 415 | 441 | 468 | 7 |
| 18 | | | | | 124 | 150 | 177 | 203 | 228 | 258 | 288 | 318 | 349 | 379 | 409 | 440 | 470 | 500 | 530 | 2 |
| 19 | | | | | | | 197 | | | | | | | | | | | | | 5 |
| 20 | | | | | | | | 197 | 228 | 288 | 322 | 356 | 390 | 425 | 459 | 494 | 528 | 562 | 597 | 1 |
| 21 | | | | | | | | | 319 | 357 | 396 | 434 | 473 | 512 | 550 | 589 | 627 | 666 | | 2 |
| 22 | | | | | | | | | 351 | 394 | 437 | 480 | 523 | 566 | 609 | 652 | 695 | 738 | | 1 |
| 23 | | | | | | | | | 385 | 433 | 480 | 528 | 576 | 624 | 671 | 719 | 767 | 814 | | -- |
| 24 | | | | | | | | | | 473 | 526 | 578 | 631 | 683 | 736 | 788 | 841 | 894 | | 1 |
| 25 | | | | | | | | | | 515 | 573 | 630 | 688 | 746 | 803 | 861 | 918 | 976 | | -- |
| 26 | | | | | | | | | | 559 | 622 | 685 | 748 | 810 | 873 | 936 | 999 | 1,062 | | -- |
| 27 | | | | | | | | | | 604 | 673 | 741 | 809 | 878 | 946 | 1,014 | 1,083 | 1,151 | | -- |
| 28 | | | | | | | | | | 652 | 726 | 800 | 873 | 947 | 1,021 | 1,095 | 1,169 | 1,243 | | -- |
| 29 | | | | | | | | | | 700 | 780 | 860 | 940 | 1,020 | 1,100 | 1,179 | 1,259 | 1,339 | | -- |

^{1/} From weighted regression: $V = 98.7701 + 0.02022 D^2 H - 0.77651 D^2 - 1.63023 H$

Standard error of estimate around mean volume ± 19.6 bd. ft. $\pm 14.8\%$

Volume, in 16-foot logs, between a one-foot stump and a merchantable top equal to 40% of d.b.h. but not less than 6.0 inches inside bark.

^{2/} Whole-inch class (e.g., $11.0 \leq 11 < 12.0$)

^{3/} Mid-point class (e.g., $57.6 \leq 60 < 62.6$)

^{4/} Lines contain basic data for 162 trees at least 9.0 inches d.b.h. Volumes in parentheses hand adjusted.

Table 4. --Volume table for quaking aspen and paper birch in Alaska ^{1/}

(In cubic feet, by Smalian's rule)

| D.b.h., D ^{2/} | Total height, H (feet) ^{3/} | | | | | | | | | | | Basis: | |
|----------------------------|--------------------------------------|------|------|------|------|------|------|------|------|------|----|---------------|--------------------------|
| | 30 | 35 | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | : trees | : measured ^{4/} |
| Inches | | | | | | | | | | | | : Aspen/birch | Number |
| 5 | 1.0 | 1.3 | 1.7 | 2.0 | 2.3 | 2.7 | 3.0 | 3.3 | | | | | 18/5 |
| 6 | 1.8 | 2.2 | 2.7 | 3.2 | 3.7 | 4.1 | 4.6 | 5.1 | 5.5 | 6.0 | | | 13/24 |
| 7 | 2.7 | 3.3 | 4.0 | 4.6 | 5.2 | 5.8 | 6.4 | 7.1 | 7.7 | 8.3 | | | 23/20 |
| 8 | 3.8 | 4.5 | 5.4 | 6.2 | 7.0 | 7.8 | 8.6 | 9.4 | 10.2 | 11.0 | | | 22/15 |
| 9 | 5.9 | 7.0 | 8.0 | 8.9 | 9.9 | 10.9 | 11.9 | 12.9 | 13.9 | 14.9 | | | 27/17 |
| 10 | 7.5 | 8.7 | 9.9 | 11.2 | 12.4 | 13.6 | 14.8 | 16.0 | 17.2 | 18.4 | | | 15/15 |
| 11 | | 10.6 | 12.1 | 13.6 | 15.0 | 16.5 | 18.0 | 19.4 | 20.9 | 21.4 | | | 12/13 |
| 12 | | 14.5 | 16.2 | 18.0 | 19.7 | 21.4 | 23.1 | 24.8 | 26.6 | | | | 13/3 |
| 13 | | | 19.1 | 21.1 | 23.1 | 25.1 | 27.1 | 29.1 | 31.1 | | | | 4/4 |
| 14 | | | 22.2 | 24.5 | 26.8 | 29.1 | 31.4 | 33.8 | 36.1 | | | | 6/3 |
| 15 | | | 25.5 | 28.1 | 30.8 | 33.4 | 36.1 | 38.7 | 41.4 | | | | 1/2 |
| 16 | | | 29.0 | 32.0 | 35.0 | 38.0 | 41.0 | 44.0 | 47.0 | | | | -/7 |
| 17 | | | | 36.1 | 39.5 | 42.9 | 46.2 | 49.6 | 53.0 | | | | -/5 |
| 18 | | | | 40.5 | 44.2 | 48.0 | 51.8 | 55.6 | 59.4 | | | | -/3 |
| 19 | | | | 45.1 | 49.3 | 53.5 | 57.7 | 61.8 | 66.0 | | | | -/1 |
| 20 | | | | | 54.6 | 59.2 | 63.8 | 68.5 | 73.1 | | | | -- |
| 21 | | | | | 60.1 | 65.2 | 70.3 | 75.4 | 80.5 | | | | -- |
| 22 | | | | | 66.0 | 71.5 | 77.1 | 82.7 | 88.2 | | | | -- |

^{1/} From weighted regression: $V = -1.024, 11 + 0.002, 203, 407, 5 D^2 H$.Standard error of estimate around mean volume ± 1.71 cu.ft. $\pm 13.8\%$; $R^2 = 0.960$.

Volume, inside bark, between a one-foot stump and a minimum merchantable top of 4.0 inches inside bark.

^{2/} Whole-inch class (e.g., $11.0 \leq 11 < 12.0$).^{3/} Mid-point class (e.g., $57.6 \leq 60 < 62.6$).^{4/} Lines contain basic data for 154 aspen and 147 birch at least 5.0 inches d.b.h.

Table 5.--Volume table for quaking aspen and paper birch in Alaska ^{1/}
(In board feet, International 1/4-inch)

| D.b.h., D ^{2/} | Total height, H (feet) ^{3/} | | | | | | | | | | Basis: | |
|----------------------------|--------------------------------------|----|-----|-----|-----|-----|-----|-----|-----|-------------|---------|--------------------------|
| | | | | | | | | | | | : trees | : measured ^{4/} |
| Inches | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | Aspen-birch | Number | |
| 11 | 33 | 41 | 49 | 57 | 65 | 73 | 81 | 88 | 96 | | 12/13 | |
| 12 | | 54 | 63 | 73 | 82 | 91 | 101 | 110 | 119 | | 13/3 | |
| 13 | | | 79 | 90 | 100 | 111 | 122 | 133 | 144 | | 4/4 | |
| 14 | | | 96 | 109 | 121 | 133 | 146 | 158 | 171 | | 6/3 | |
| 15 | | | 113 | 128 | 142 | 156 | 171 | 185 | 199 | | 1/2 | |
| 16 | | | 132 | 149 | 165 | 181 | 197 | 214 | 230 | | -/7 | |
| 17 | | | | 171 | 189 | 208 | 226 | 244 | 262 | | -/5 | |
| 18 | | | | 194 | 215 | 235 | 256 | 276 | 296 | | -/3 | |
| 19 | | | | | 242 | 265 | 287 | 310 | 322 | | -/1 | |
| 20 | | | | | 271 | 296 | 321 | 346 | 371 | | -- | |
| 21 | | | | | 301 | 328 | 356 | 383 | 411 | | -- | |
| 22 | | | | | 332 | 362 | 392 | 423 | 455 | | -- | |

^{1/} From weighted regression: $V = -29.8848 + 0.011,913,084 D^2H$
Standard error of estimate around mean volume ± 25.4 bd. ft. $\pm 21.1\%$;
 $R^2 = 0.806$.

Volume, in 16-foot logs, between a one-foot stump and a merchantable top equal to 40% of d.b.h. but not less than 8.0 inches inside bark.

^{2/} Whole-inch class (e.g. $11.0 \leq 11 < 12.0$).

^{3/} Mid-point class (e.g. $57.6 \leq 60 < 62.6$).

^{4/} Lines contain basic data for 36 aspen and 41 birch at least 11.0 inches d.b.h.

Table 6. --Volume table for quaking aspen and paper birch in Alaska ^{1/}
(In board feet, Scribner)

| D.b.h.: D ^{2/} | Total height, H (feet) ^{3/} | | | | | | | | | | Basis: trees : measured ^{4/} | |
|----------------------------|--------------------------------------|----|-----|-----|-----|-----|-----|-----|-----|----|--|---------|
| | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | 85 | : aspen/birch | Number |
| Inches | | | | | | | | | | | | |
| 11 | 26 | 32 | 39 | 45 | 52 | 58 | 65 | 72 | 78 | | | 12 / 13 |
| 12 | | 43 | 51 | 58 | 66 | 74 | 82 | 89 | 97 | | | 13 / 3 |
| 13 | | | 64 | 73 | 82 | 91 | 100 | 109 | 118 | | | 4 / 4 |
| 14 | | | 77 | 88 | 98 | 109 | 119 | 130 | 140 | | | 6 / 3 |
| 15 | | | 92 | 104 | 116 | 128 | 140 | 152 | 164 | | | 1 / 2 |
| 16 | | | 108 | 122 | 135 | 149 | 162 | 176 | 190 | | | - / 7 |
| 17 | | | | 140 | 156 | 171 | 186 | 201 | 217 | | | - / 5 |
| 18 | | | | 160 | 177 | 194 | 211 | 228 | 245 | | | - / 3 |
| 19 | | | | | 200 | 219 | 238 | 257 | 276 | | | - / 1 |
| 20 | | | | | 224 | 245 | 266 | 286 | 307 | | | - / - |
| 21 | | | | | 249 | 272 | 295 | 318 | 341 | | | - / - |
| 22 | | | | | 275 | 300 | 325 | 351 | 376 | | | - / - |

^{1/} From weighted regression: $V = -27.163 + .00995 D^2H$.

Standard error of estimate around mean volume ± 21.0 bd. ft. $\pm 21.2\%$.
Volume, in 16-foot logs, between a one-foot stump and a merchantable top equal to 40% of d.b.h. but not less than 8.0 inches inside bark.

^{2/} Whole-inch class (e.g., $11.0 \leq 11 < 12.0$)

^{3/} Mid-point class (e.g., $57.6 \leq 60 < 62.6$)

^{4/} Lines contain basic data for 36 aspen and 41 birch at least 11.0 inches d.b.h.

Table 7.--Volume table for balsam poplar in Alaska ^{1/}

(In cubic feet, by Smalian's rule)

| D.b.h. D ^{2/} | Total height, H (feet) ^{3/} | | | | | | | | | | | | | | | | | | | Basis: trees meas- ured ^{4/} |
|---------------------------|--------------------------------------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|-----|--|
| | 30 | 35 | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | 85 | 90 | 95 | 100 | 105 | 110 | 115 | 120 | |
| Inches | 0.8 | 1.1 | 1.3 | 1.6 | 1.9 | 2.2 | 2.4 | 2.7 | | | | | | | | | | | | Number |
| 5 | 0.8 | 1.1 | 1.3 | 1.6 | 1.9 | 2.2 | 2.4 | 2.7 | | | | | | | | | | | | 3 |
| 6 | 1.4 | 1.8 | 2.2 | 2.6 | 3.0 | 3.4 | 3.7 | 4.1 | 4.5 | | | | | | | | | | | 5 |
| 7 | 2.2 | 2.7 | 3.2 | 3.7 | 4.2 | 4.8 | 5.3 | 5.8 | 6.3 | 6.8 | | | | | | | | | | 4 |
| 8 | 3.0 | 3.7 | 4.4 | 5.0 | 5.7 | 6.4 | 7.0 | 7.7 | 8.3 | 9.0 | 9.6 | 10.3 | | | | | | | | 7 |
| 9 | | 4.9 | 5.7 | 6.5 | 7.3 | 8.1 | 9.0 | 9.8 | 10.6 | 11.4 | 12.2 | 13.0 | | | | | | | | 8 |
| 10 | | 6.1 | 7.1 | 8.1 | 9.1 | 10.1 | 11.1 | 12.1 | 13.1 | 14.1 | 15.1 | 16.2 | | | | | | | | 15 |
| 11 | | 7.5 | 8.7 | 9.9 | 11.1 | 12.3 | 13.5 | 14.7 | 15.9 | 17.1 | 18.3 | 19.5 | 20.7 | 21.9 | | | | | | 7 |
| 12 | | 9.0 | 10.5 | 11.9 | 13.3 | 14.7 | 16.1 | 17.6 | 19.0 | 20.4 | 21.8 | 23.2 | 24.6 | 26.1 | | | | | | 10 |
| 13 | | 10.7 | 12.4 | 14.0 | 15.7 | 17.3 | 19.0 | 20.6 | 22.3 | 23.9 | 25.6 | 27.2 | 28.9 | 30.5 | 32.2 | 33.8 | 35.5 | 37.1 | | 5 |
| 14 | | | | 16.3 | 18.2 | 20.1 | 22.0 | 23.9 | 25.8 | 27.7 | 29.6 | 31.5 | 33.4 | 35.4 | 37.3 | 39.2 | 41.2 | 43.1 | | 6 |
| 15 | | | | 18.7 | 20.9 | 23.1 | 25.3 | 27.4 | 29.6 | 31.8 | 34.0 | 36.2 | 38.3 | 40.5 | 42.7 | 44.9 | 47.0 | 49.2 | | 8 |
| 16 | | | | 21.2 | 23.7 | 26.2 | 28.7 | 31.2 | 33.7 | 36.2 | 38.6 | 41.1 | 43.6 | 46.0 | 48.5 | 51.0 | 53.4 | 55.9 | | 5 |
| 17 | | | | 26.9 | 29.7 | 32.4 | 35.2 | 38.0 | 40.8 | 43.6 | 46.3 | 49.1 | 51.9 | 54.6 | 57.4 | 60.2 | 63.0 | | | 6 |
| 18 | | | | 33.3 | 36.4 | 39.5 | 42.6 | 45.7 | 48.8 | 51.9 | 55.0 | 58.1 | 61.2 | 64.3 | 67.4 | 70.5 | 73.6 | | | 7 |
| 19 | | | | 37.0 | 40.5 | 43.9 | 47.4 | 50.8 | 54.3 | 57.7 | 61.2 | 64.6 | 68.1 | 71.5 | 74.9 | 78.4 | 81.8 | | | 4 |
| 20 | | | | | 44.8 | 48.6 | 52.4 | 56.2 | 60.1 | 63.9 | 67.7 | 71.5 | 75.3 | 79.1 | 82.9 | 86.7 | 90.5 | | | 7 |
| 21 | | | | | 49.4 | 53.6 | 57.8 | 62.0 | 66.2 | 70.3 | 74.5 | 78.7 | 82.9 | 87.1 | 91.3 | 95.5 | 99.7 | | | 3 |
| 22 | | | | 54.2 | 58.8 | 63.4 | 68.0 | 72.5 | 77.1 | 81.7 | 86.3 | 90.9 | 95.5 | 100 | 105 | 109 | | | | 3 |
| 23 | | | | 59.2 | 64.2 | 69.2 | 74.2 | 79.2 | 84.2 | 89.2 | 94.2 | 99.2 | 104 | 109 | 114 | 119 | | | | -- |
| 24 | | | | | 75.3 | 80.7 | 86.2 | 91.6 | 97.0 | 102 | 108 | 113 | 118 | 124 | 130 | | | | | 3 |
| 25 | | | | | 81.6 | 87.5 | 93.4 | 99.3 | 105 | 111 | 117 | 123 | 129 | 135 | 141 | | | | | 3 |
| 26 | | | | 88.2 | 94.6 | 101 | 107 | 114 | 120 | 126 | 133 | 139 | 146 | 152 | | | | | | 5 |
| 27 | | | | 95.0 | 102 | 109 | 116 | 122 | 129 | 136 | 143 | 150 | 157 | 164 | | | | | | 2 |
| 28 | | | | 103 | 110 | 117 | 124 | 131 | 139 | 146 | 154 | 161 | 168 | 176 | | | | | | 2 |
| 29 | | | | | 117 | 125 | 133 | 141 | 149 | 157 | 165 | 173 | 180 | 188 | | | | | | -- |
| 30 | | | | | 134 | 142 | 151 | 159 | 167 | 176 | 184 | 193 | 201 | | | | | | | 3 |
| 31 | | | | | 143 | 152 | 161 | 170 | 179 | 188 | 197 | 206 | 215 | | | | | | | -- |
| 32 | | | | | 152 | 162 | 171 | 181 | 190 | 200 | 210 | 219 | 229 | | | | | | | -- |
| 33 | | | | | 162 | 172 | 182 | 192 | 202 | 212 | 223 | 233 | 243 | | | | | | | -- |
| 34 | | | | | 172 | 182 | 193 | 204 | 215 | 226 | 236 | 247 | 258 | | | | | | | -- |

^{1/} From weighted regression: $V = -0.8722 + 0.001,811,522 D^2H$.Standard error of estimate around mean volume ± 4.30 cu. ft. $\pm 10.1\%$; $R^2 = 0.986$.

Volume, inside bark, between a one-foot stump and a minimum merchantable top of 4.0 inches inside bark.

^{2/} Whole-inch class (e.g. $11.0 \leq 11 < 12.0$).^{3/} Mid-point class (e.g. $57.6 \leq 60 < 62.6$).^{4/} Lines contain basic data for 131 trees at least 5.0 inches d.b.h.

Table 8.--Volume table for balsam poplar in Alaska ^{1/}

(In board feet, International 1/4-inch)

| D.b.h. D ₂ | Total height, H (feet) ^{3/} | | | | | | | | | | | | | | | | Basis: trees meas- ured ^{4/} | Number |
|--------------------------|--------------------------------------|----|-----|-----|-----|-----|-----|-----|-----|-------|-------|-------|-------|-------|-------|-------|--|--------|
| | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | 85 | 90 | 95 | 100 | 105 | 110 | 115 | 120 | |
| 11 | 9 | 16 | 23 | 31 | 38 | 45 | 52 | 60 | 67 | 74 | 82 | 89 | | | | | | 7 |
| 12 | 19 | 28 | 36 | 45 | 54 | 62 | 71 | 79 | 88 | 96 | 105 | 113 | | | | | | 10 |
| 13 | 31 | 41 | 51 | 61 | 71 | 81 | 91 | 101 | 111 | 121 | 131 | 141 | 151 | 161 | 171 | 181 | | 5 |
| 14 | | 55 | 67 | 78 | 89 | 101 | 112 | 123 | 135 | 147 | 158 | 170 | 181 | 193 | 205 | 216 | | 6 |
| 15 | | 70 | 83 | 96 | 109 | 122 | 135 | 148 | 161 | 174 | 188 | 201 | 214 | 227 | 231 | 244 | | 8 |
| 16 | | 85 | 100 | 115 | 130 | 145 | 160 | 174 | 189 | 204 | 219 | 234 | 249 | 264 | 279 | 294 | | 5 |
| 17 | | | 118 | 135 | 152 | 169 | 186 | 203 | 219 | 236 | 253 | 270 | 286 | 303 | 320 | 337 | | 6 |
| 18 | | | | 157 | 176 | 194 | 213 | 232 | 251 | 269 | 288 | 307 | 326 | 344 | 363 | 382 | 401 | 7 |
| 19 | | | | 180 | 201 | 222 | 242 | 263 | 284 | 305 | 326 | 346 | 367 | 388 | 409 | 430 | 451 | 4 |
| 20 | | | | | 227 | 250 | 273 | 296 | 319 | 342 | 365 | 388 | 411 | 434 | 457 | 480 | 502 | 7 |
| 21 | | | | | 255 | 280 | 305 | 330 | 356 | 381 | 406 | 431 | 457 | 482 | 508 | 533 | 558 | 3 |
| 22 | | | | | 283 | 311 | 339 | 366 | 394 | 422 | 449 | 477 | 505 | 533 | 561 | 588 | 616 | 3 |
| 23 | | | | | 313 | 343 | 374 | 404 | 434 | 465 | 495 | 525 | 556 | 586 | 616 | 646 | 676 | -- |
| 24 | | | | | | | 411 | 444 | 476 | 509 | 542 | 575 | 608 | 641 | 674 | 706 | 739 | 3 |
| 25 | | | | | | | 449 | 485 | 520 | 556 | 592 | 627 | 663 | 699 | 734 | 769 | 805 | 3 |
| 26 | | | | | | | 489 | 527 | 566 | 604 | 643 | 682 | 720 | 758 | 796 | 835 | 873 | 5 |
| 27 | | | | | | | 530 | 572 | 613 | 654 | 696 | 737 | 779 | 820 | 861 | 902 | 944 | 2 |
| 28 | | | | | | | 573 | 618 | 662 | 706 | 751 | 796 | 840 | 884 | 928 | 973 | 1,018 | 2 |
| 29 | | | | | | | | 665 | 713 | 760 | 808 | 855 | 903 | 951 | 999 | 1,046 | 1,094 | -- |
| 30 | | | | | | | | | 765 | 816 | 867 | 918 | 969 | 1,020 | 1,071 | 1,122 | 1,173 | 3 |
| 31 | | | | | | | | | 820 | 874 | 928 | 982 | 1,036 | 1,091 | 1,145 | 1,200 | 1,254 | -- |
| 32 | | | | | | | | | 876 | 933 | 991 | 1,049 | 1,107 | 1,165 | 1,223 | 1,280 | 1,338 | -- |
| 33 | | | | | | | | | 933 | 995 | 1,056 | 1,117 | 1,179 | 1,240 | 1,302 | 1,363 | 1,425 | -- |
| 34 | | | | | | | | | 993 | 1,058 | 1,123 | 1,188 | 1,254 | 1,319 | 1,384 | 1,449 | 1,514 | -- |

^{1/} From weighted regression: $V = -49.1199 + 0.010,941,441 D^2H$.Standard error of estimate around mean volume ± 47.7 bd. ft. $\pm 15.2\%$; $R^2 = 0.954$.

Volume, in 16-foot logs, between a one-foot stump and a merchantable top equal to 40% of d.b.h. but not less than 8.0 inches inside bark.

^{2/} Whole-inch class (e.g., $11.0 \leq 11 < 12.0$).^{3/} Mid-point class (e.g., $57.6 \leq 60 < 62.6$).^{4/} Lines contain basic data for 89 trees at least 11.0 inches d.b.h.

Table 9.--Volume table for balsam poplar in Alaska^{1/}
(In board feet, Scribner)

| | | Total height, H (feet) ^{3/} | | | | | | | | | | | | | | | | Basis: | | |
|--------|----|--------------------------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-------|-------|-------|-------|-------|-------|--------|-------|-------------------------|
| | | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | 85 | 90 | 95 | 100 | 105 | 110 | 115 | 120 | trees | meas-ured ^{4/} |
| Inches | | Number | | | | | | | | | | | | | | | | | | |
| 11 | 4 | 10 | 16 | 23 | 29 | 35 | 42 | 48 | 54 | 61 | 67 | 73 | | | | | | | 7 | |
| 12 | 13 | 20 | 28 | 35 | 43 | 50 | 58 | 65 | 73 | 80 | 88 | 95 | | | | | | | 10 | |
| 13 | 23 | 32 | 40 | 49 | 58 | 66 | 75 | 84 | 93 | 101 | 110 | 119 | 128 | 136 | 145 | 154 | | | 5 | |
| 14 | | 44 | 54 | 64 | 74 | 84 | 94 | 104 | 114 | 124 | 134 | 144 | 154 | 164 | 174 | 184 | | | 6 | |
| 15 | | 57 | 68 | 80 | 91 | 102 | 114 | 126 | 137 | 148 | 160 | 172 | 183 | 194 | 206 | 217 | | | 8 | |
| 16 | | 70 | 83 | 96 | 109 | 122 | 135 | 148 | 162 | 174 | 188 | 200 | 214 | 226 | 240 | 253 | | | 5 | |
| 17 | | | 100 | 114 | 129 | 144 | 158 | 173 | 188 | 202 | 217 | 231 | 246 | 261 | 275 | 290 | | | 6 | |
| 18 | | | | 133 | 150 | 166 | 182 | 199 | 215 | 231 | 248 | 264 | 280 | 297 | 313 | 330 | 346 | | 7 | |
| 19 | | | | 153 | 171 | 190 | 208 | 226 | 244 | 262 | 280 | 299 | 317 | 335 | 353 | 371 | 390 | | 4 | |
| 20 | | | | | 194 | 214 | 234 | 255 | 275 | 295 | 315 | 335 | 355 | 375 | 395 | 415 | 435 | | 7 | |
| 21 | | | | | | 218 | 240 | 263 | 285 | 307 | 329 | 351 | 373 | 395 | 417 | 439 | 462 | 484 | 3 | |
| 22 | | | | | | 244 | 268 | 292 | 316 | 340 | 365 | 389 | 413 | 437 | 461 | 486 | 510 | 534 | 3 | |
| 23 | | | | | | 270 | 296 | 323 | 349 | 376 | 402 | 428 | 454 | 481 | 508 | 534 | 560 | 587 | --- | |
| 24 | | | | | | | 355 | 384 | 412 | 441 | 470 | 498 | 527 | 556 | 584 | 613 | 642 | | 3 | |
| 25 | | | | | | | 388 | 420 | 451 | 482 | 513 | 544 | 575 | 606 | 637 | 668 | 699 | | 3 | |
| 26 | | | | | | | 423 | 457 | 490 | 524 | 558 | 591 | 625 | 658 | 692 | 725 | 759 | | 5 | |
| 27 | | | | | | | 459 | 496 | 532 | 568 | 604 | 640 | 676 | 712 | 748 | 785 | 821 | | 2 | |
| 28 | | | | | | | 497 | 536 | 574 | 613 | 652 | 691 | 730 | 769 | 807 | 846 | 885 | | 2 | |
| 29 | | | | | | | | 577 | 619 | 660 | 702 | 744 | 785 | 827 | 868 | 910 | 952 | | --- | |
| 30 | | | | | | | | | 665 | 709 | 754 | 798 | 843 | 887 | 932 | 976 | 1,020 | | 3 | |
| 31 | | | | | | | | | 712 | 760 | 807 | 854 | 902 | 949 | 997 | 1,044 | 1,092 | | --- | |
| 32 | | | | | | | | | 761 | 812 | 862 | 912 | 963 | 1,014 | 1,064 | 1,114 | 1,165 | | --- | |
| 33 | | | | | | | | | 812 | 865 | 919 | 972 | 1,026 | 1,080 | 1,133 | 1,187 | 1,241 | | --- | |
| 34 | | | | | | | | | 864 | 920 | 977 | 1,034 | 1,091 | 1,148 | 1,205 | 1,262 | 1,319 | | --- | |

^{1/} From weighted regression: $V = -46.7415 + 0.00956 D^2H$

Standard error of estimate around mean volume ± 40.1 bd. ft. $\pm 14.6\%$

Volume, in 16-foot logs, between a one-foot stump and a merchantable top equal to 40% of d.b.h. but not less than 8.0 inches inside bark.

^{2/} Whole-inch class (e.g. 11.0 \leq 11 < 12.0)

^{3/} Mid-point class (e.g. 57.6 \leq 60 < 62.6)

^{4/} Lines contain basic data for 89 trees at least 11.0 inches d.b.h.

